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Sealing Elements, Precision Mechanics, Tools,
Specific Electronic Equipment & Mechatronics
HERVEX 2023**

Baile Govora, ROMANIA | 8-10 November, 2023



**A milestone moment:
CELEBRATING
30 YEARS TOGETHER!**

**IMPACT VELOCITY CONTROL OF HOPKINSON BAR
MECHATRONICS SYSTEM USING DRIVING ROBUST
PRESSURE, NUMERICAL CALIBRATION, STRAIN WAVE
MEASUREMENT AND INVERSE ANALYSIS**

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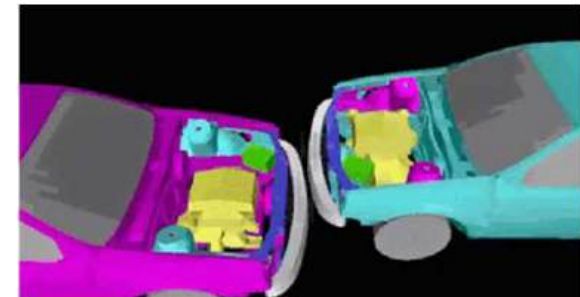
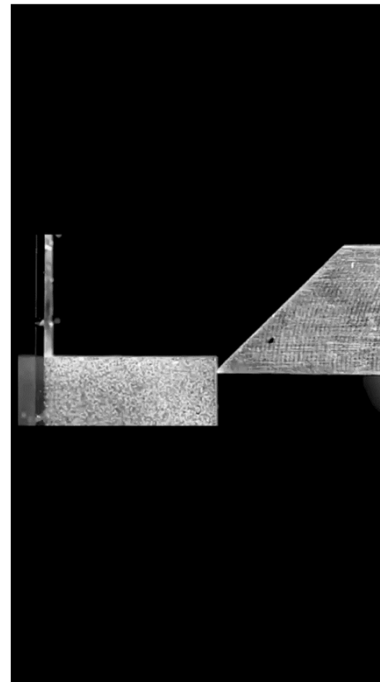
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1. Introduction

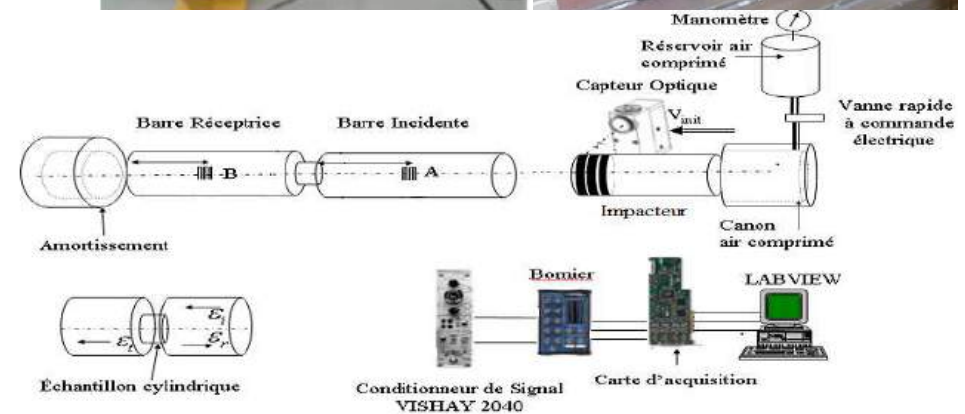
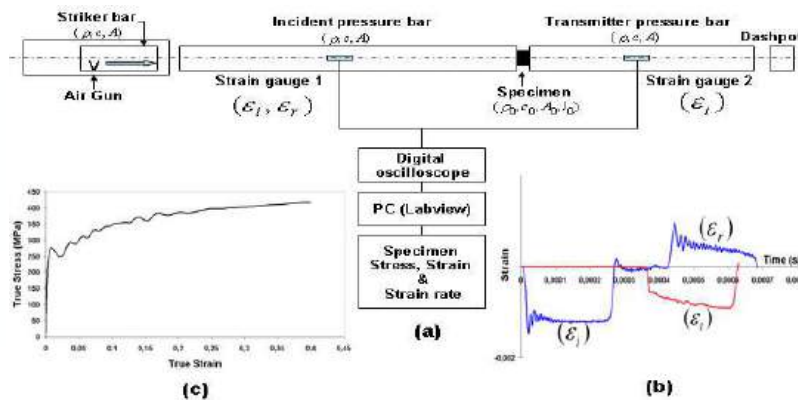
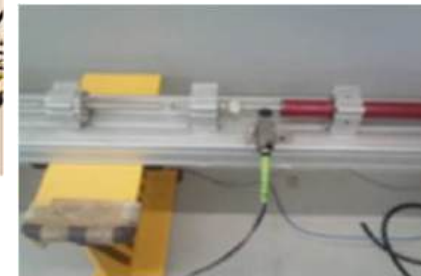
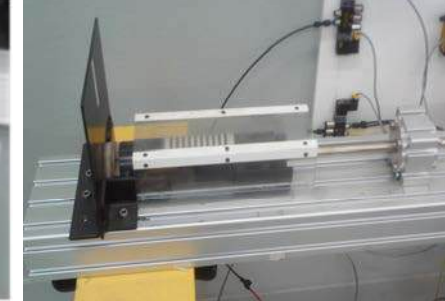
Industrial Processes under Severe or Complex Loadings: Rapid Forging, High Speed Machining, Friction or Laser Welding, Automotive Crash, Impact, ...



Process Optimisation using Numerical Simulation

$$\bar{\sigma} = \sigma_0(\bar{\varepsilon}, \dot{\bar{\varepsilon}}, T, \dots) \quad \text{for} \quad \dot{\bar{\varepsilon}} \propto \mathbf{v}_{car} / l_{car} \in [10^{-3} \text{ s}^{-1}, 10^5 \text{ s}^{-1}]$$

2. Pneumatic SHPB Mechatronics System



2.1 Framework and SHPB design characteristics

Table 1: Material and geometric characteristics of SHPB bars (total length of bench support $\approx 5,5$ m)

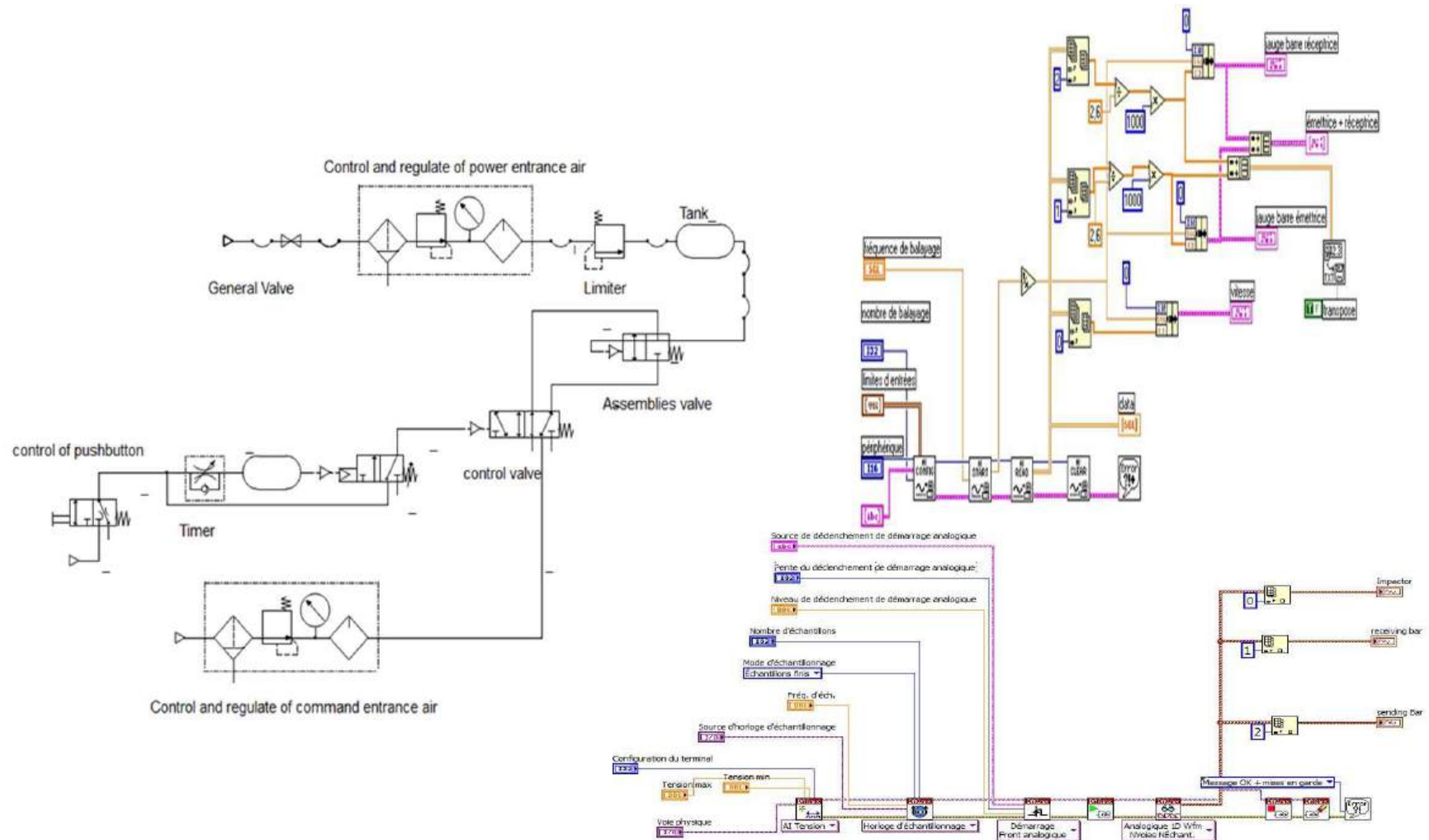
Bars	Air Gun	Striker Bar	Receiving Bar	Sending Bar
Material	MARVAL 18	MARVAL 18	MARVAL 18	MARVAL 18
Diameter [mm]	$\phi_{in} 30.0$ and $\phi_{out} 40.0$	$\phi 16.0$	$\phi 16.0$	$\phi 16.0$
Length [m]	2.0	0.602 (0.5÷1)	2.0	1.3

Table 2: Elastic mechanical properties of MARVAL 18 steel bars

Temperature 20°C	E_b [GPa]	ν	$R_{0,2}$ [MPa]	ρ_b [Kg /m ³]	$c_b = \sqrt{E_b / \rho_b}$ [m/s]	$Z_b = \rho_b c_b = \sqrt{\rho_b E_b}$ [Kg/m ² s]
MARVAL 18	186	0,33	1840	8000	4821,82	$38,57 \cdot 10^6$

$\bar{\epsilon}_{max} \approx \ln \left[1 - (2v_{imp} l_{b_{imp}} / l_0 c_b) \right]^{-1}$. Considering a cylindrical specimen with a length $l_0 = 10$ mm and an initial impact velocity $v_{imp} = 10$ m/s a value of $\bar{\epsilon}_{max}$ around of 25%-50% can be obtained for $l_{b_{imp}} \in [0.5m, 1m] \Rightarrow l_{bi} \geq 1m + 2m$ and $l_{be} \geq 0.5m + 1m$. More great plastic deformations of specimen, especially for smallest impact velocities, can be obtain for shorter specimens or specimens with special or unconventional local shape as dumbbell sample or hat one. To minimize effect of the radial dispersion elastic waves and to have bars elastic deformations conditions close to the infinite wave propagation theory [7], the bars diameters d_b must to be very small as compared to the twist of striker bar lengths i.e. $d_b / c_b t_i = d_b / 2l_{b_{imp}} \ll 1$. The Table 1 and Table 2 synthetize the chosen material and geometric characteristics of INSA Rennes Hopkinson bars in order to perform compression impact tests with large plastic deformations of material specimen at high strain rates (more than $500s^{-1} - 1000s^{-1}$ corresponding to $v_{imp} \in [10m / s, 30m / s]$).

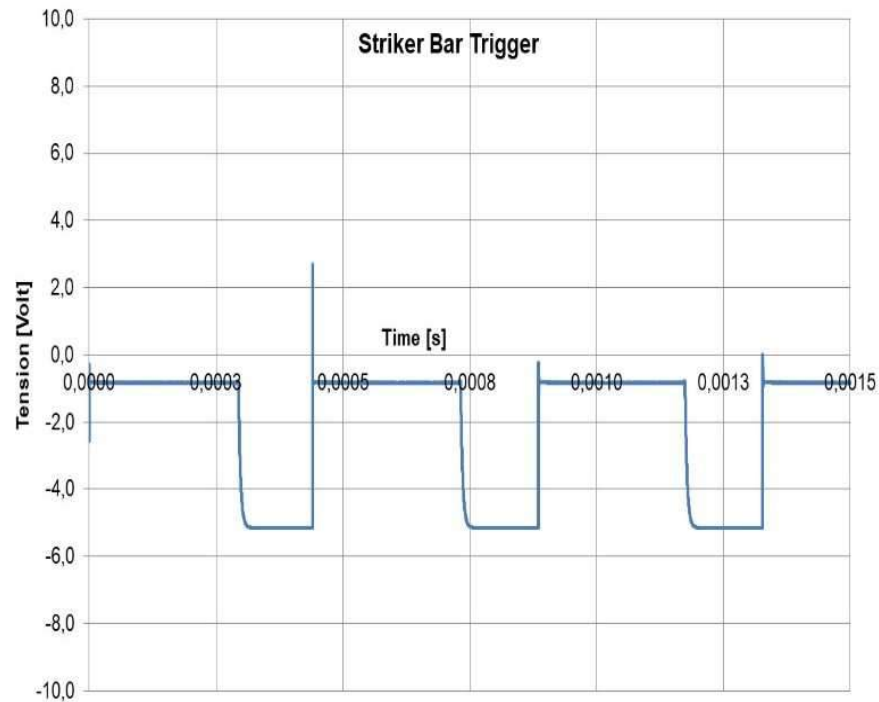
2.2 Pneumatic control circuit and experimental data acquisition



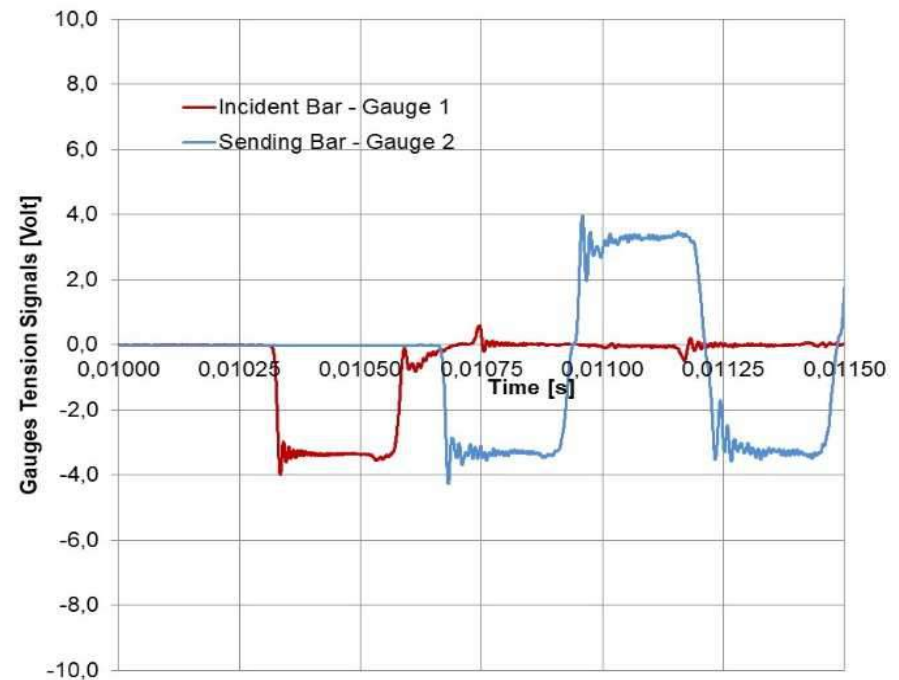
2.2 Pneumatic control circuit and experimental data acquisition

Fig.4. a) Square-Shaped Dirac tension signal of laser optical camera recorded by triggering option using Labview program, b) Gauges tension signal variation corresponding to the elastic wave deformation of the incident bar ($\varepsilon_i(t)$, $\varepsilon_r(t)$ for red curve) and sending bar ($\varepsilon_t(t)$ for blue curve) corresponding to a set tank air pressure of 1,9 bars - 2 bars [16]

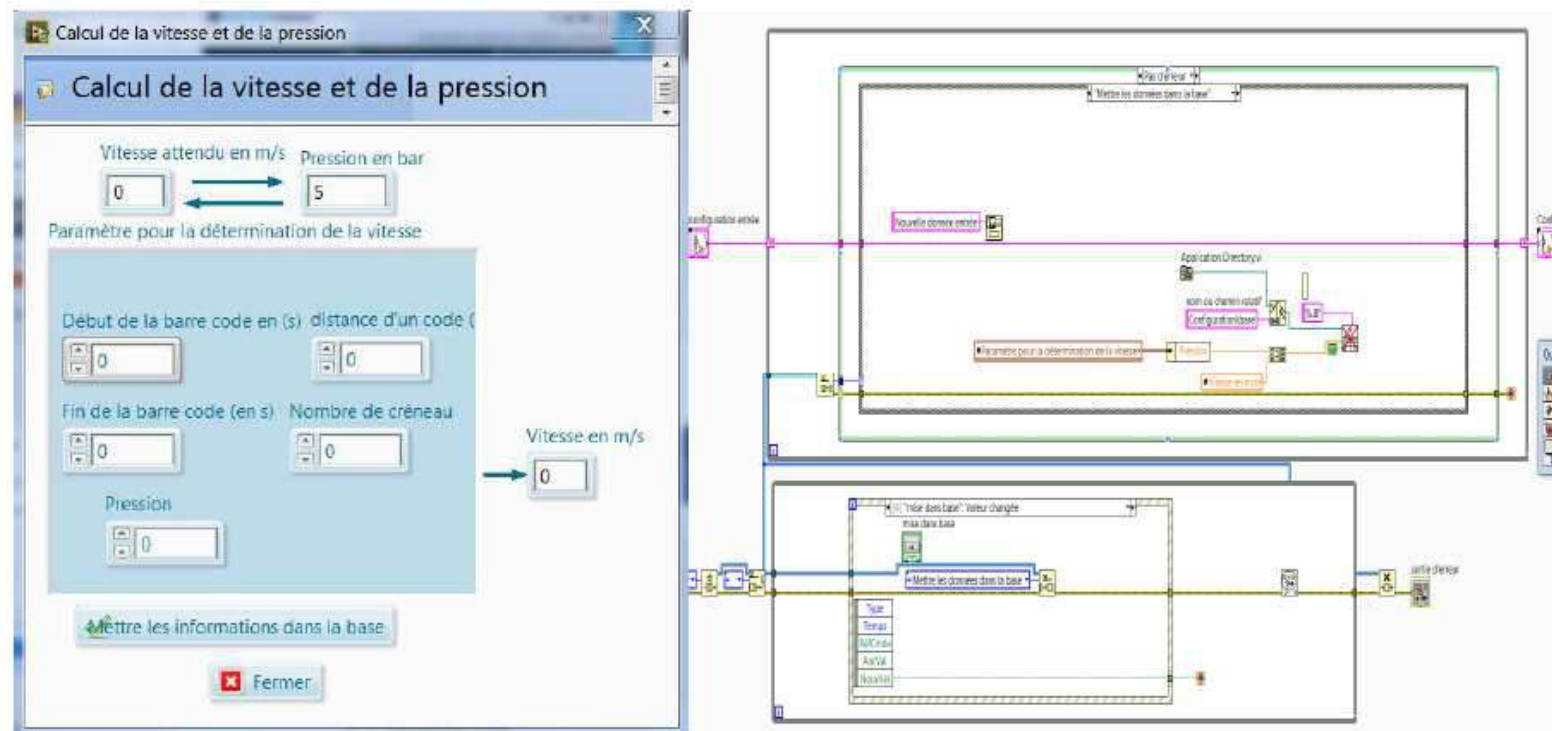
$$v = \lambda_v / T_v \approx 10 \text{ m/s} \quad \lambda_v = 5 \text{ mm}$$



$$K_{\text{exp}} = \varepsilon / \hat{U} \text{ (}\mu\text{def/Volt)} \quad \varepsilon \approx 2\hat{U} \cdot 10^6 / U_0 G F_g (1 + \nu)$$



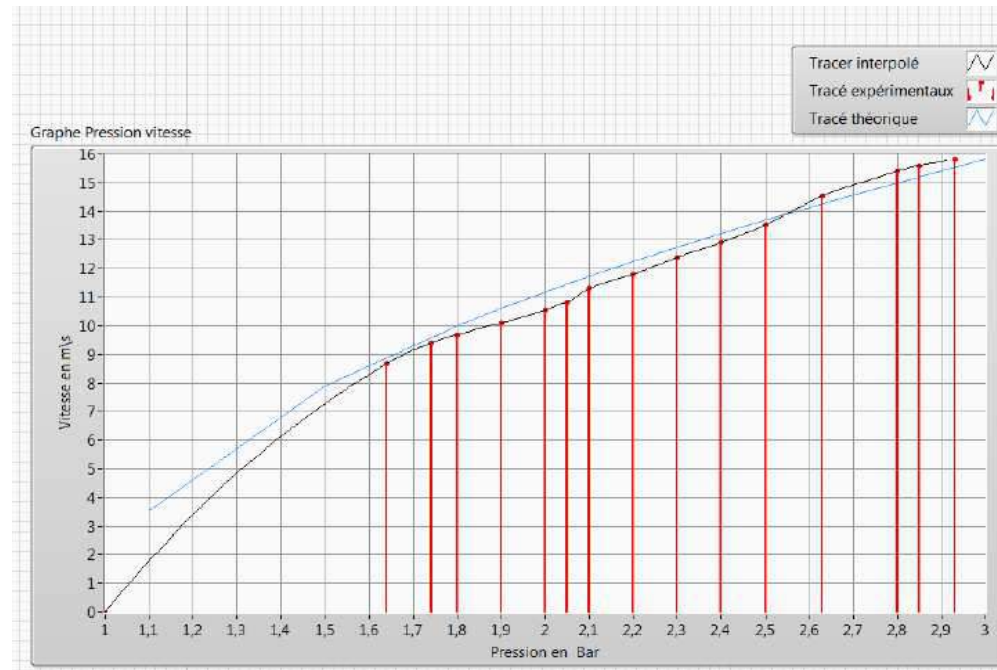
2.3 Experimental estimation of initial impact velocity using Hermite interpolation method



2.3 Experimental estimation of initial impact velocity using Hermite interpolation method

$$P_i(x) = f(x_i) + (x - x_i) [f'(x_i) - q'_i(x_i) f(x_i)] \quad q_i(x) = \prod_{j=0, j \neq i}^{j=n} \left(\frac{x - x_j}{x_i - x_j} \right)^2$$

$$P(x) = \sum_{i=0}^n q_i(x) P_i(x)$$



2.4 Theoretical estimation of initial impact velocity "v"

$$\Delta E_c + E_f = \frac{1}{2}mv^2 + E_f = W = \int_0^l \left(\iint p(x) dS \right) dx$$

$$p(x)(V_0 + Sx) = p_r V_0$$

$$W = \int_0^l p(x) S dx = \int_0^l \left(\frac{p_r V_0 S}{V_0 + Sx} \right) dx = p_r V_0 \ln \left(1 + \frac{lS}{V_0} \right)$$

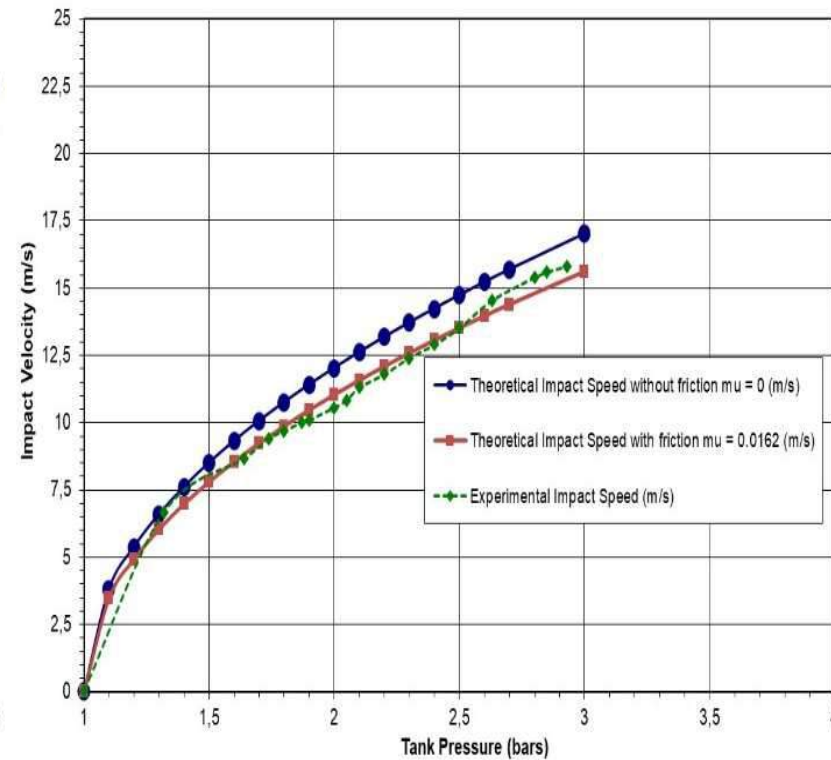
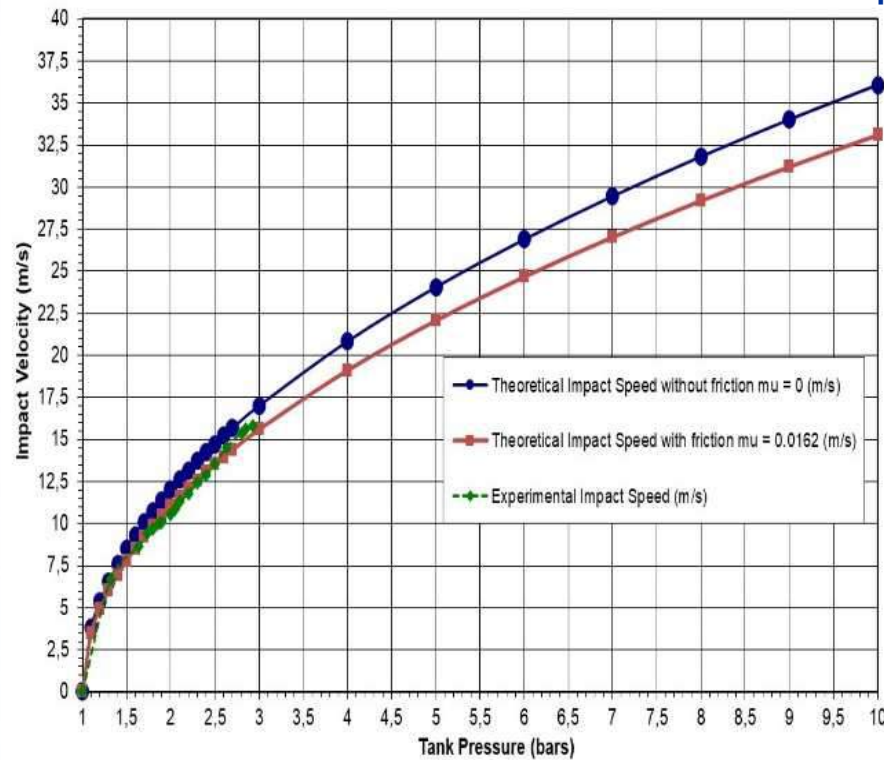
$$\Delta E_f = \int_0^L F_f dx', F_f = \mu \pi D n_f, n_f = p(x) \exp(-4\mu x' / D), E_f = \int_0^l \Delta E_f dx$$

$$v = \sqrt{\frac{2V_0}{m} \ln \left(1 + \frac{lS}{V_0} \right) \exp(-4\mu L / D) \cdot \sqrt{(p_c - p_0)}}$$

$$v = \left(\alpha' / \sqrt{l_{imp}} \right) \sqrt{(p_c - p_0)}$$

2.4 Theoretical estimation of initial impact velocity "v"

$l_{imp} = 0,602 \text{ m}$

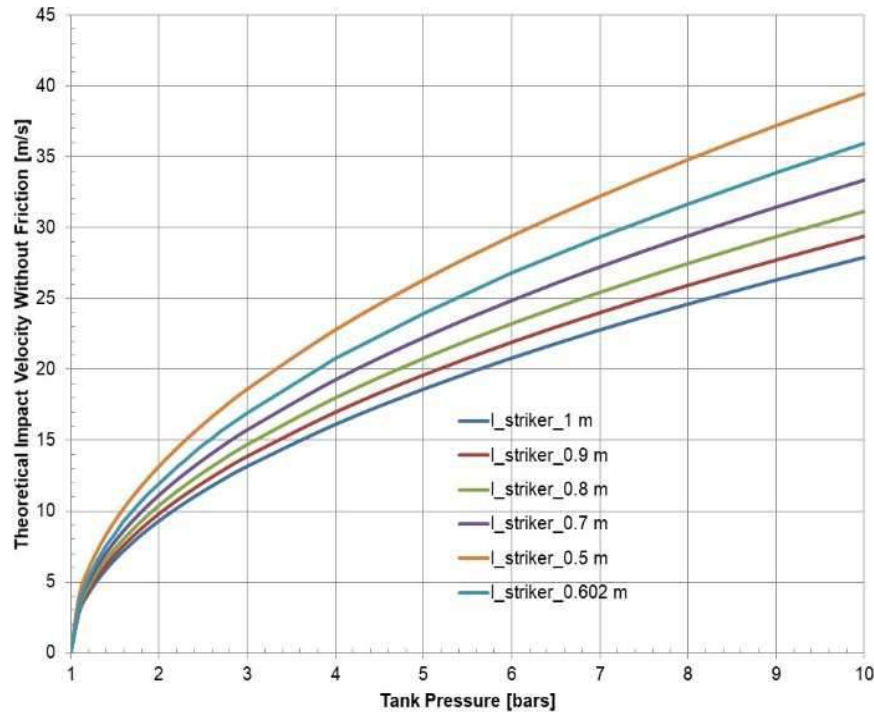


$$\text{Min}_{\mu} \left[\left(\sum_{i=1}^{N_{exp}} (v - v^{exp})^2 \right) / \sum_{i=1}^{N_{exp}} v^{exp^2} \right]$$

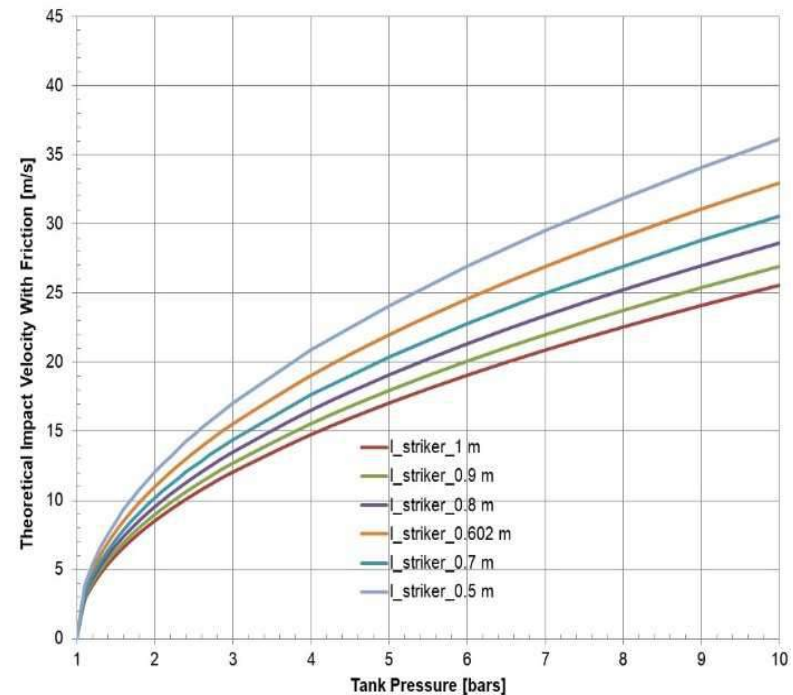
$$\mu = 0,0162$$

The identification error of friction coefficient is around of 3%.

2.4 Theoretical estimation of initial impact velocity "v"



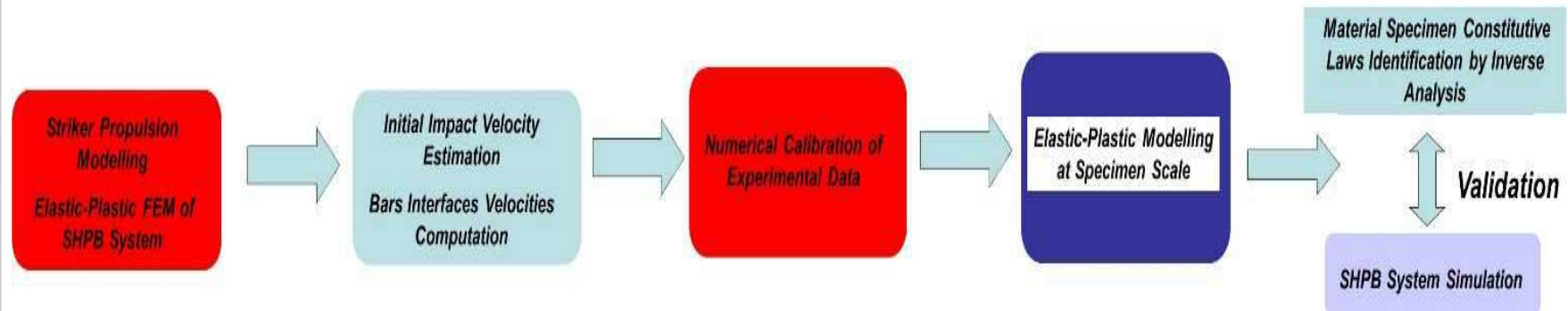
$$\mu = 0$$



$$\mu = 0,0162$$

An average estimation error of 8 % is obtained c

3. Numerical Analysis

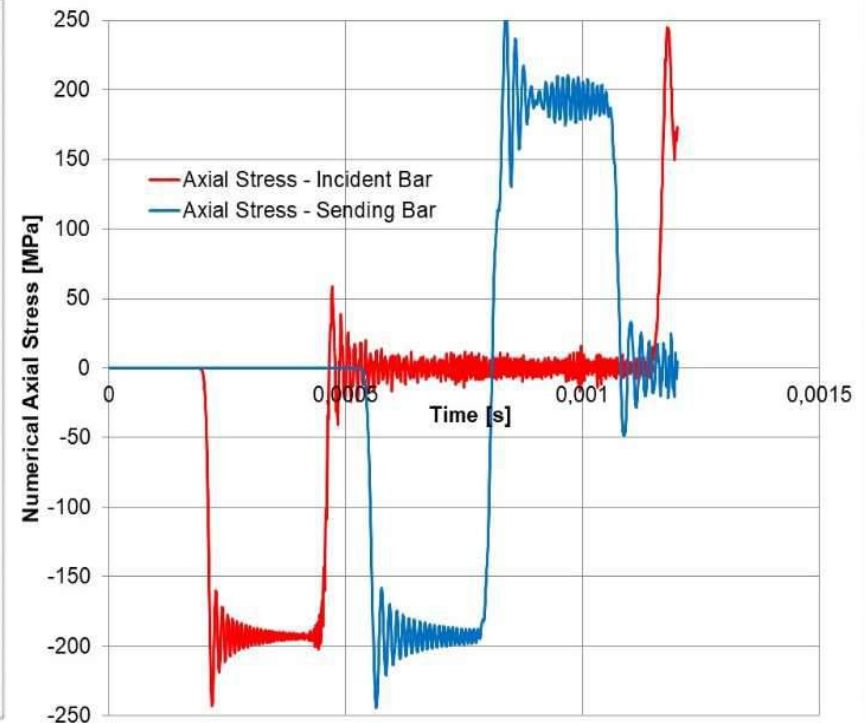
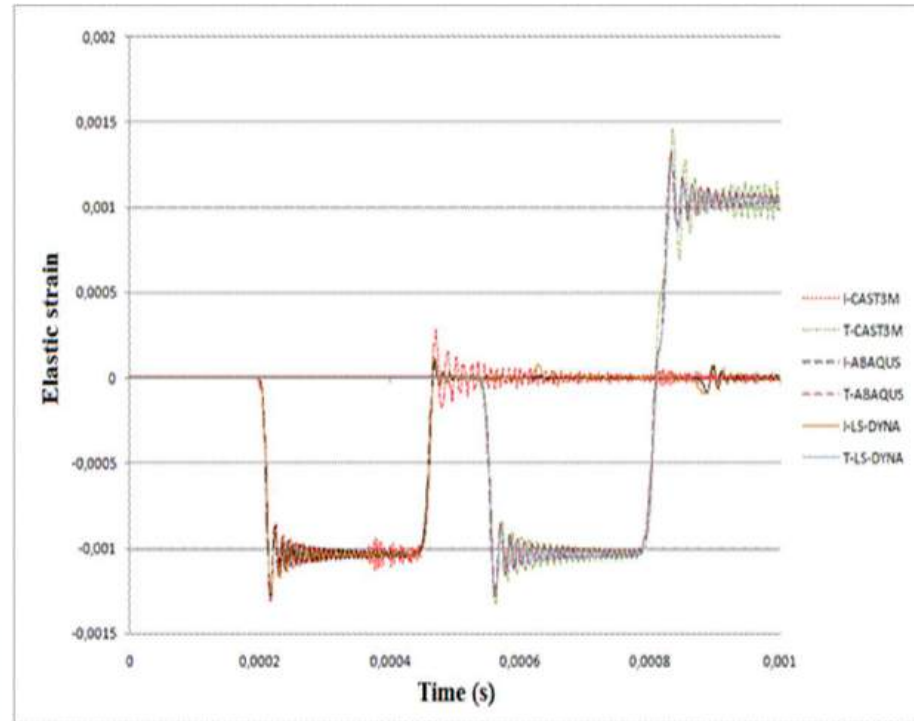


An axisymmetric dynamic Finite Element Modelling of SHPB test choosing an initial impact velocity of 10 m/s and an incremental time of 10^{-6} s is performed using Cast3M [18], ABAQUS and LS-Dyna code [9-13, 14-15] based on tridimensional elastic properties of the bars, inertial effect and QUAD4 mesh (Figure 10).



Fig.10. Mesh of the striker, incident and sending bars used for a Dynamic Finite Element Simulation of the SHPB device using Cast3M, Abaqus and LS-Dyna code

3.1 Numerical Calibration and FEM of SHPB System



$$K_{an} = v \cdot 10^6 / 2c_{exp} \hat{U}_i (\mu def / Volt)$$

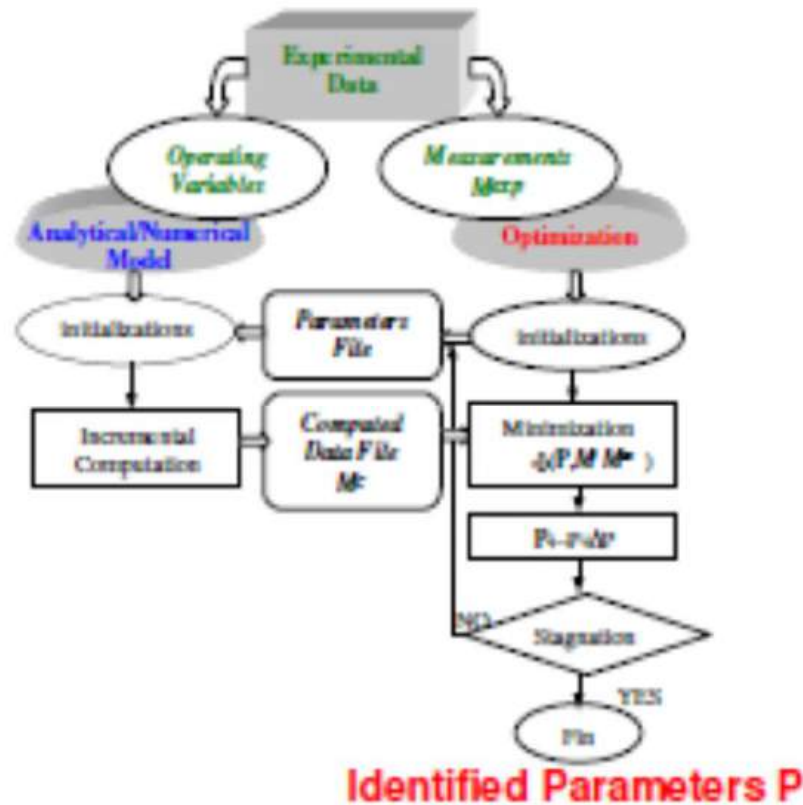
$$K_{num} = \hat{\varepsilon}_{i_num} / \hat{U}_i (\mu def / Volt)$$

$$K_{exp} = 384,62 \mu def / Volt.$$

$$K_{an} = 317 \mu def / Volt$$

$$K_{num} = 310,7 \mu def / Volt$$

3.2 Numerical Inverse Analysis of SHPB System



$$\Phi(P) = \frac{\sum_{k=1}^{N_{exp}} [M^c(P) - M^a]^2}{\sum_{k=1}^{N_{exp}} [M^{exp}]^2}$$

or

$$\Phi(P) = \sum_{k=1}^{N_{exp}} \left[\frac{M^c(P) - M^a}{M^a} \right]^2$$

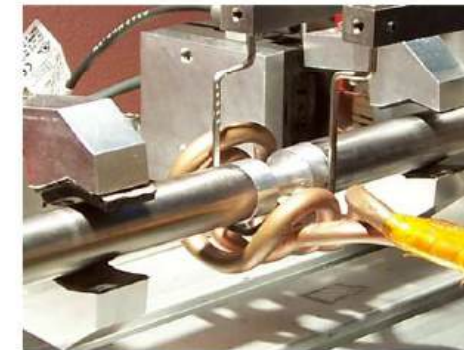
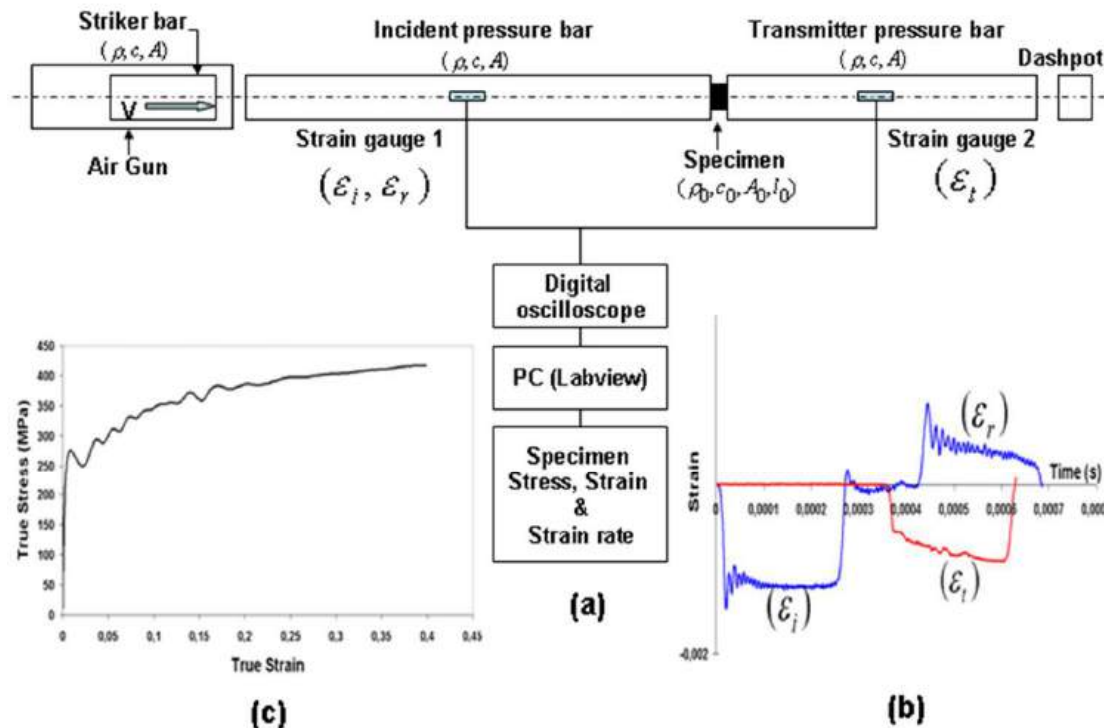
**GAUSS-NEWTON OR LEVENBERG-MARQUARD
MINIMISATION ALGORITHM**

$$[\Delta P] = - \left[\frac{d^2\Phi}{dP^2} \right]^{-1} \left[\frac{d\Phi}{dP} \right]$$

SHPB TEST

(Gavrus, 2000-2008 – HDR; Caestecker, 2003; Davoodi, 2006 – PhD Thesis LGCGM)
(collaboration with Mechanical Laboratory of Tampere University - Finlande)

CLASSICAL PRINCIPLE OF COLD OR HOT SHPB UPSETTING



Classical Analytical
Analysis using Elastic
Wave Theory to estimate

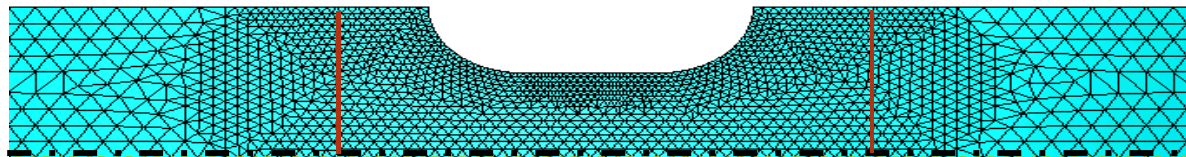
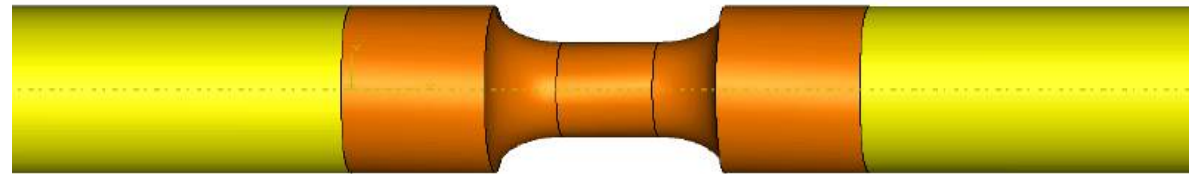
$$\bar{\sigma}^{exp}, \bar{\epsilon}^{exp}, \dot{\bar{\epsilon}}^{exp}$$

• *Neglecting the contact friction and the heterogeneity of the deformation*

• *Use of non-linear REGRESSION to identify law parameters*

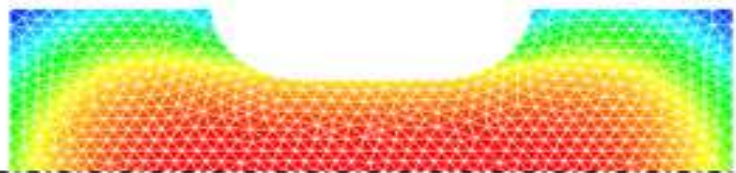
FEM SIMULATION AND INVERSE ANALYSIS OF SHPB TEST

COMPLETE NUMERICAL SIMULATION



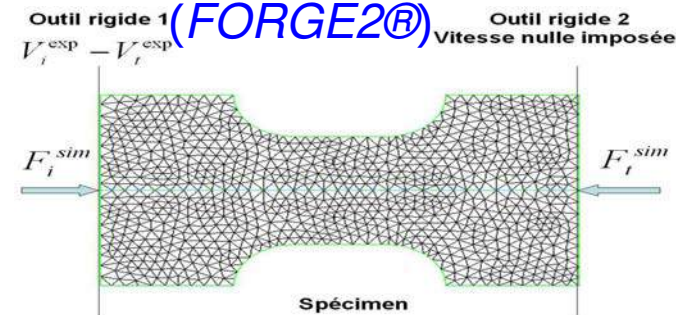
THERMAL SIMULATION
(CAST3M)

(Initial Heating: 500°C and Cooling 10 s)



(Tmax = 483.72 °C, Tmin = 482.723°C)

INVERSE ANALYSIS OF A REDUCED MODEL
(FORGE2®)



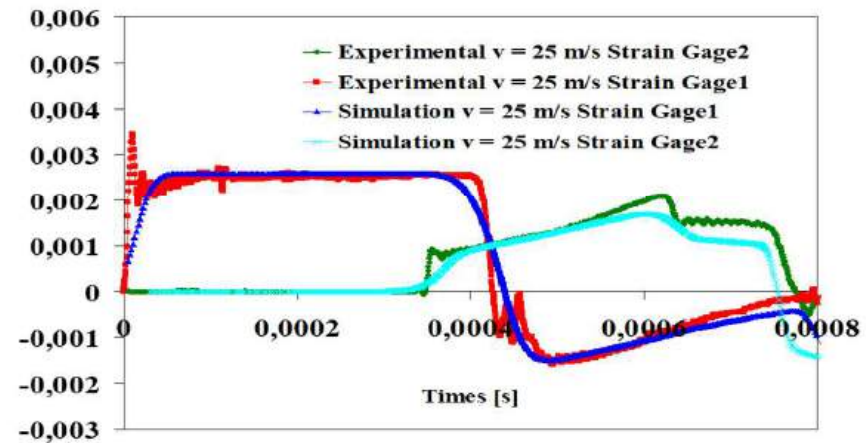
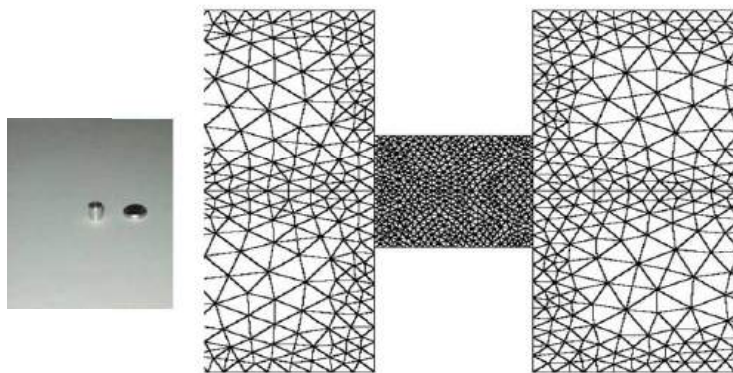
$$Q(P) = \frac{\sum_{K=1}^M \left[F_{i_k}^{sim}(P) - F_{i_k}^{ex} \right]^2}{\sum_{K=1}^M \left[F_{i_k}^{ex} \right]^2} + \frac{\sum_{K=1}^M \left[F_{t_k}^{sim}(P) - F_{t_k}^{ex} \right]^2}{\sum_{K=1}^M \left[F_{t_k}^{ex} \right]^2}$$

PARAMETER IDENTIFICATION BY INVERSE ANALYSIS OF THE SHPB REDUCED MODEL

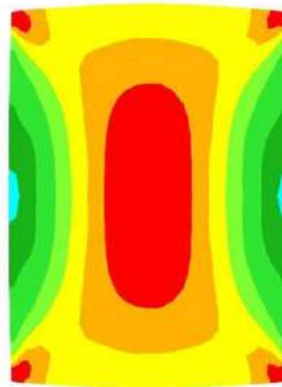
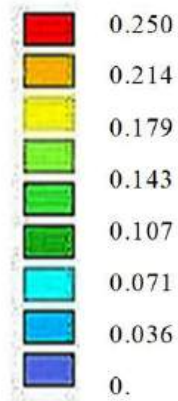
Parameters Identified Values using different constitutive laws (Johnson-Cook, Cowper-Symonds, ASH, ...) for the AA5083 aluminium alloy ($A = \sigma_{00} = 142 \text{ MPa}$, $T_r = 293 \text{ °K}$, $T_m = 933 \text{ °K}$)

		Parameters P								Q (%)	Nb Iter
		B	n_0	n_1	n	C_0	C_1	C	m		
Law I (JC)	Init.	500,	-	-	0,250	-	-	0,001	2,00	29	10
	final	118,	-	-	0,281	-	-	0,093	1,935	7,07	
Law II	Init.	118,	0,280	0,00	-	0,090	0,00	-	1,930	7,17	7
	final	122,	0,504	-0,0005	-	0,166	-0,0002	-	2,996	6,99	
Law III	Init.	500,	-	-	1,00	-	-	0,001	2,00	13,9	17
	final	98,6	-	-	14,382	-	-	0,073	1,969	6,61	
Law IV	Init.	98,6	14,380	0,00	-	0,073	0,00	-	1,970	6,62	16
	final	99,3	1,936	0,026	-	0,148	-0,0002	-	4,692	6,29	
Law V	Init.	120,	-	-	0,300	-	-	0,100	2,000	15,9	11
	final	82,4	-	-	0,401	-	-	0,104	1,970	7,47	
Law VI	Init.	82,4	0,400	0,00	-	0,100	0,00	-	1,970	7,53	10
	final	108	1,083	-0,0015	-	0,224	-0,0003	-	1,975	7,12	

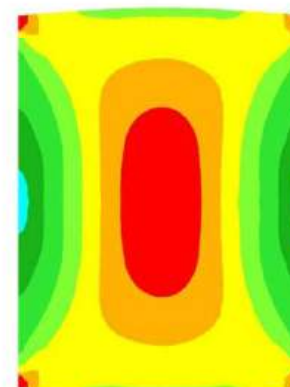
COMPLETE SIMULATION USING AN IMPLICIT NUMERICAL FEM (FORGE2®)



COMPARAISON BETWEEN COMPLETE MODEL (a) AND REDUCED MODEL (b)

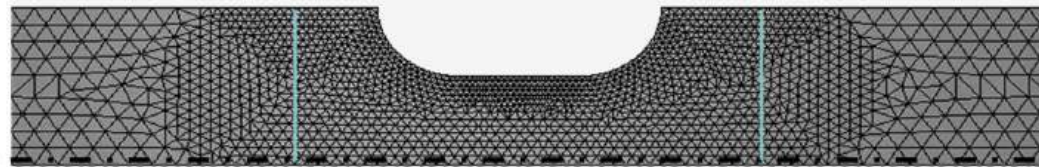


a)

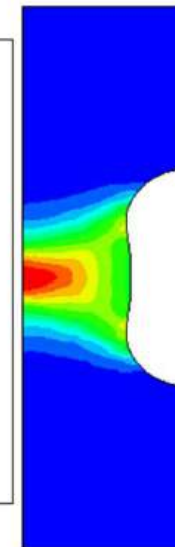
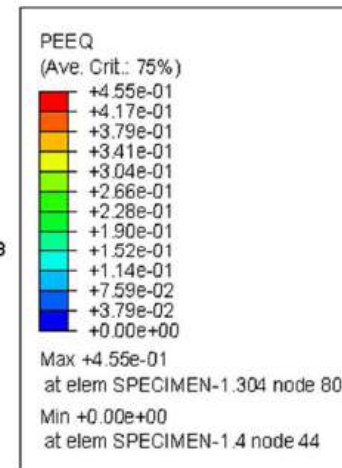
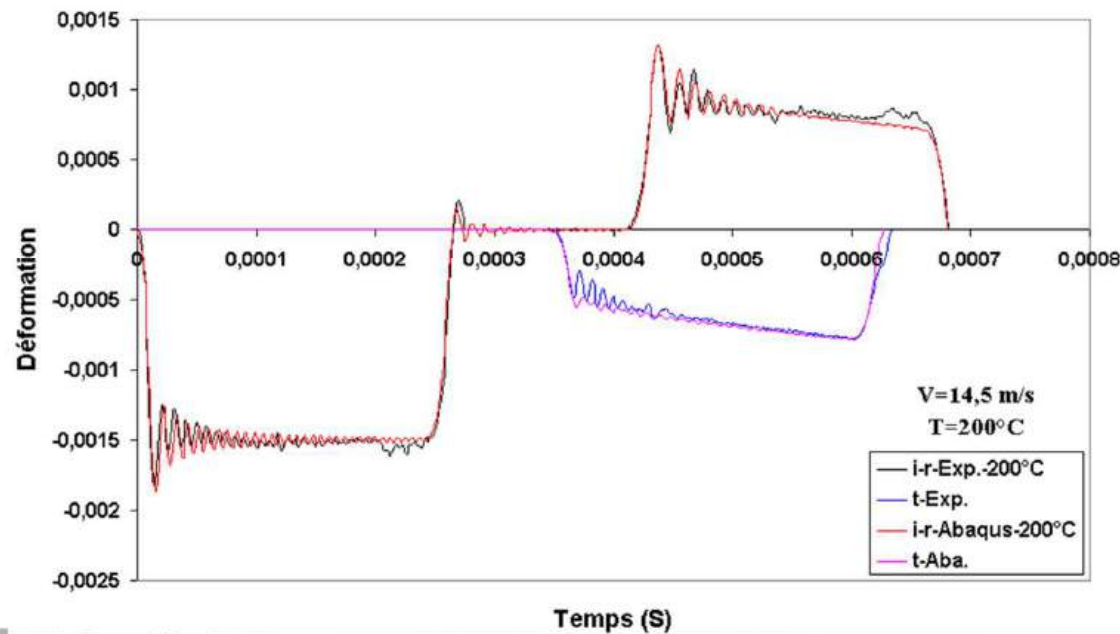


b)

COMPLETE SIMULATION USING AN EXPLICIT NUMERICAL FEM (ABAQUS)

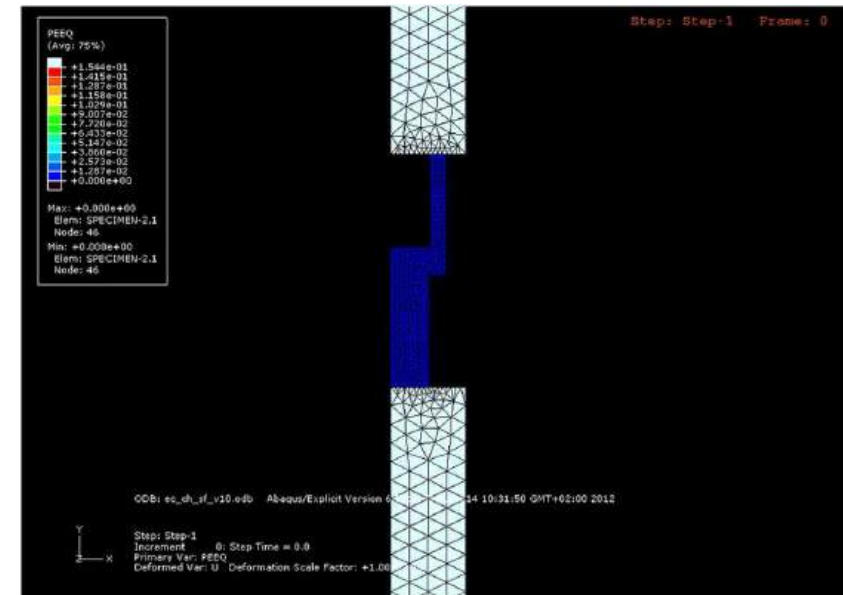
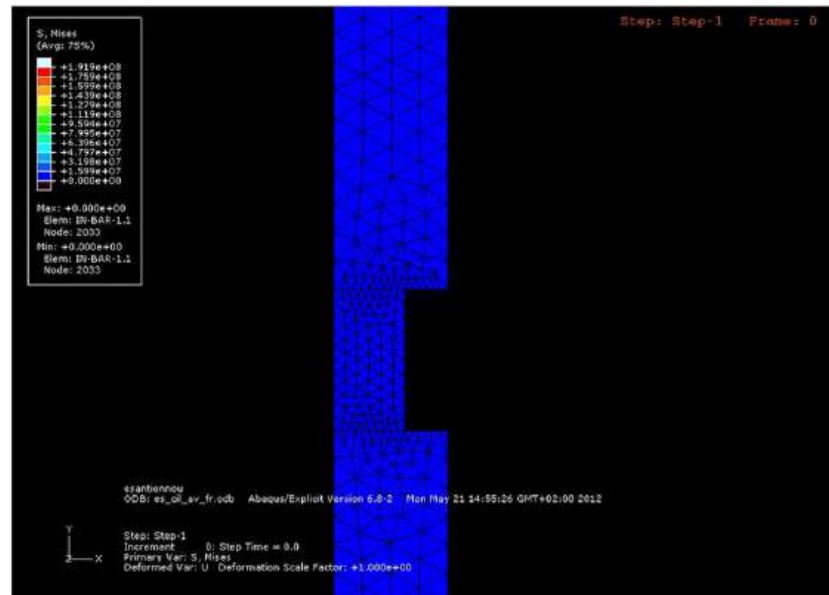


$$\bar{\sigma} = [142 + 118,68 \bar{\epsilon}^{0,2814}] / [1 + 0,093 \ln \dot{\bar{\epsilon}}] / [1 - (\frac{T - 293}{933 - 293})^{1,935}]$$



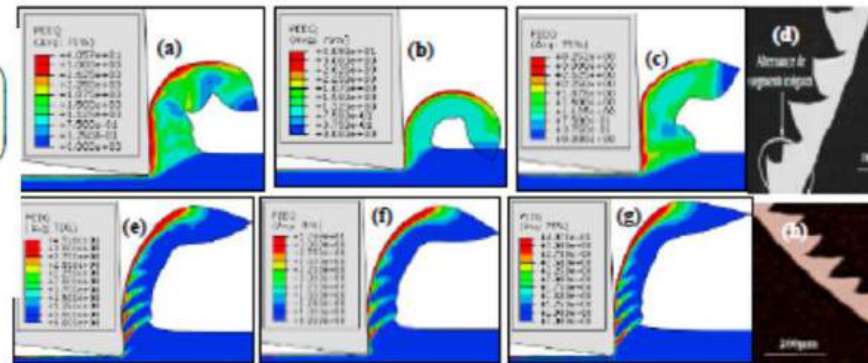
V=14,5 m/s, T=200 °C

SHPB Finite Element Simulations



Applications to High Speed Machining

$$\sigma = \left(\sigma_0 + B \times [1 - \exp(-n \times \varepsilon)]^{1/n} \right) \times \left(1 + ASH \left[0.5 \times \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)^c \right] \right) \times \left(1 - k \times \left(\frac{T - T_R}{T_M - T_R} \right)^m \right)^j \quad \text{if } T_R \leq T < T_R + (T_M - T_R) \left(\frac{1}{k} \right)^{1/m}$$

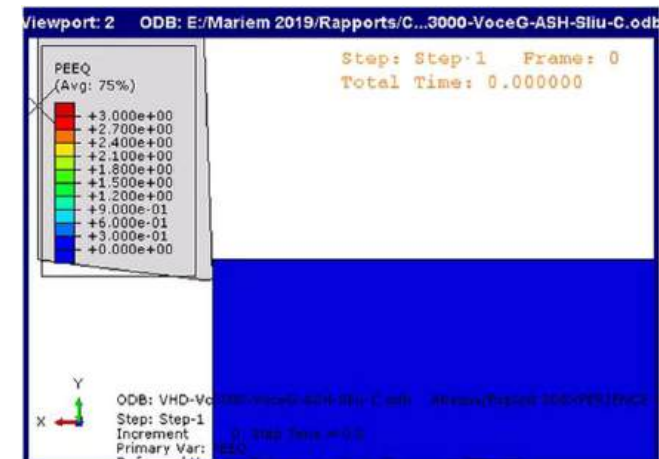
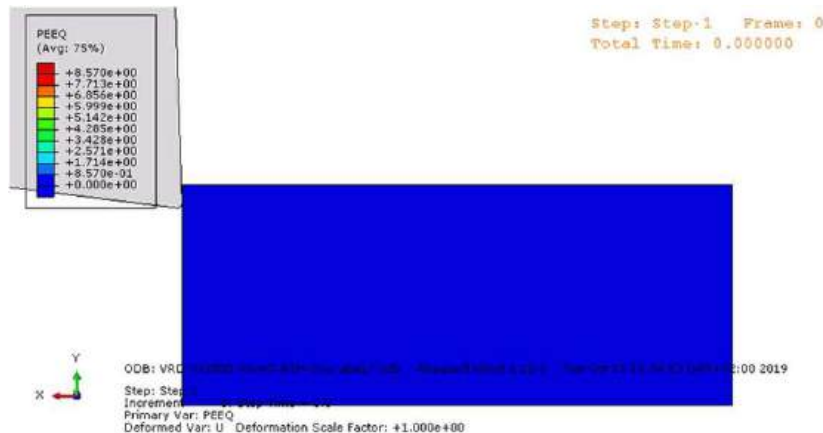


60 m/min

180 m/min

60 m/min

180 m/min



1. Conclusion and Perspectives

- The above experimental design and quantitative description of the pneumatic compression mechatronic SHPB bench confirms the robustness of impact speeds control together with strong validations of their theoretical dependency on tank air pressure set.
- A new hybrid analytical-numerical calibration method was detailed in order to can estimate the elastic wave strains which travels with a specific celerity the incident and sending bars.
- A complete dynamic Finite Element Modelling and Simulation of the SHPB system without specimen has been performed to establish a more rigorous estimation of the conversion factor between the measured gauge full bridge tension and real elastic strain value.
- Comparisons with analytical formula based on elastic wave propagation theory of infinite bars have shown the high precision of the Finite Element Modelling results, which permit to valid the entire calibration strategy.
- It is also possible to confirm again the rightness of the proposed Two-Step Inverse Analysis technique developed from 1998 during previous research works at INSA Rennes to identify specific constitutive equations of metallic materials under severe loadings and complex deformation paths: large plastic strains, high strain rates, temperature influence and important local gradients of thermo-mechanical variables.
- Regarding the generality of the proposed numerical calibration method, this one will be apply in a future research work to improve the SHPB acquisition system by use of local Bragg optic fibers sensors and specific optical interrogators developed by Dimione Systems of France and Redondo Optics Company of USA to measure in a more accuracy manner the elastic deformations of the bars.

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